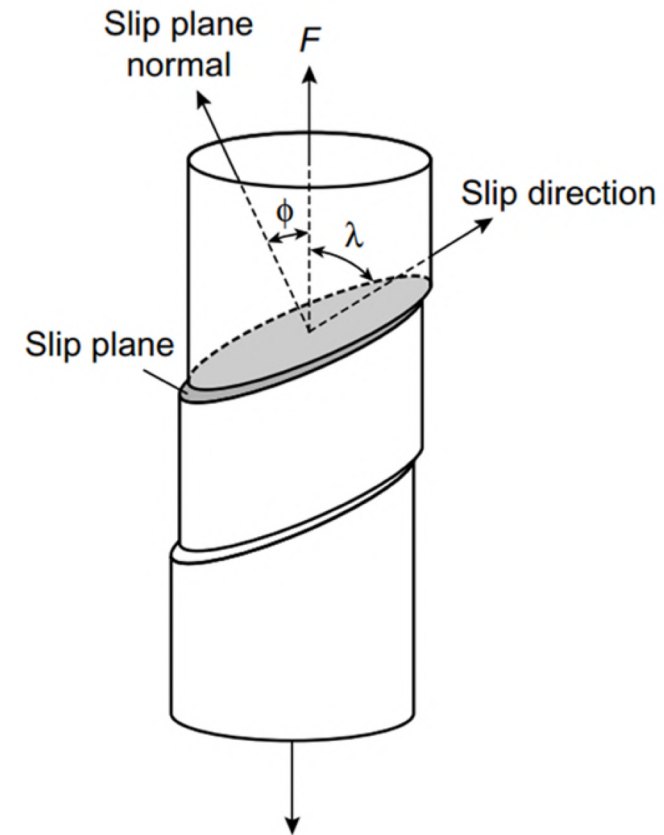


Course goal: Describe deformation and annealing behaviour in terms of slip, twinning and recrystallization mechanisms. And recall the activities of the different slip and twinning systems and how they change with temperature.

## Learning outcomes:

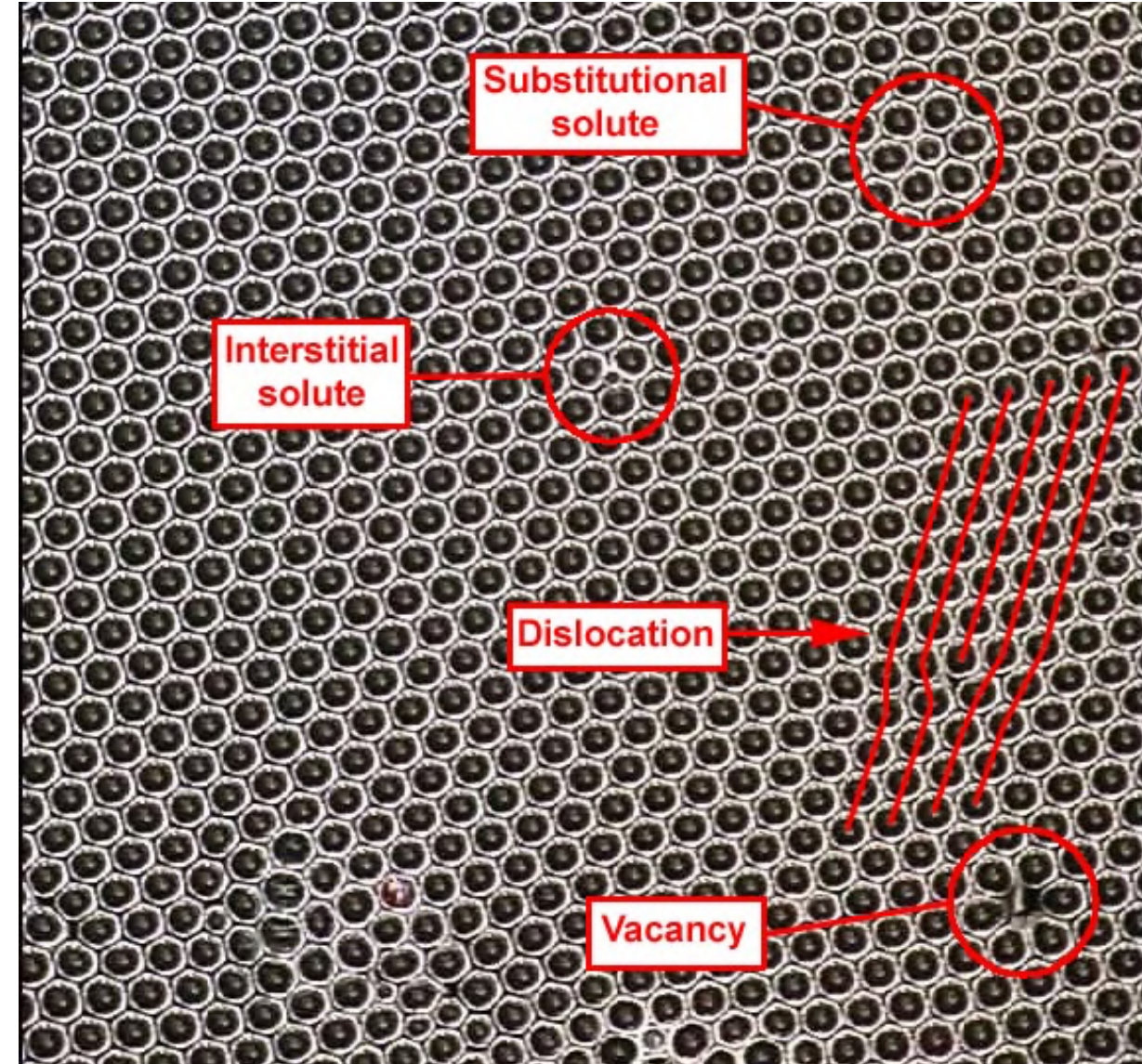
- ***Explain how slip contributes to grain reorientation and recall equations for RSS, CRSS and Schmid Factor.***
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- Explain how twinning contributes to grain reorientation and recall the main twinning types in Ti and Zr alloys.
- Describe the driving forces for recrystallization and recovery processes in terms of boundary and stored energy.



Schematic of applied forces acting on a slip plane during tensile deformation

## Dislocations

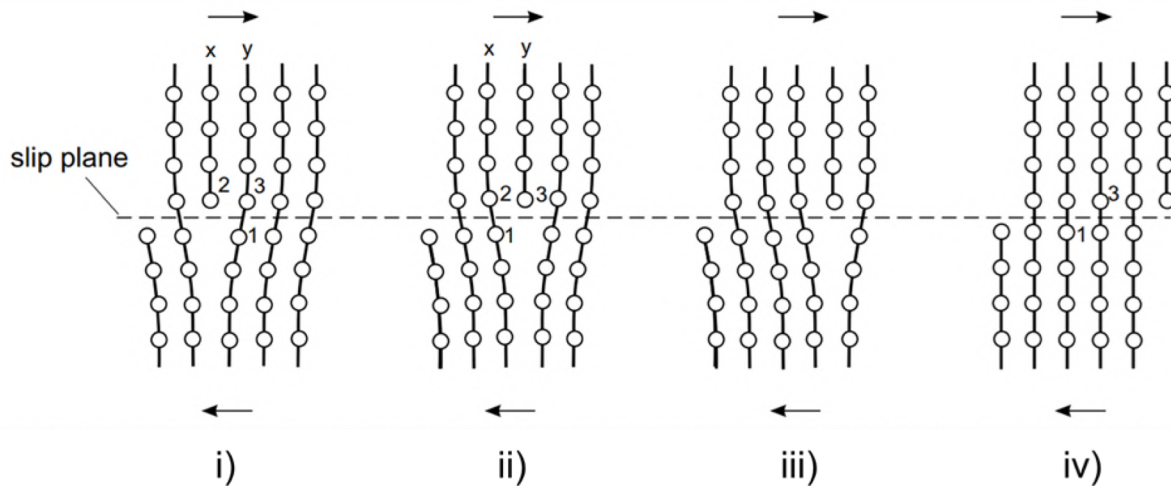
- **Grain boundary** – interface between two regions with different crystal orientation.
- **Vacancy** – point defect when atom 'missing' from lattice.
- **Solute atom** – different atomic species.
  - *Substitutional solute*: similar in size substituting for host atom
  - *Interstitial solute*: smaller in size than host and sit in gaps (interstices) of host lattice.
- **Dislocation** – Extra 'half-row' of atoms, characterised by Burgers vector ( $\mathbf{b}$ ) giving orientation and magnitude.
- **Dislocation type** – defined by alignment with line vector ( $\mathbf{l}$ ). Edge type ( $\mathbf{b} \parallel \mathbf{l}$ ). Screw type ( $\mathbf{b} \perp \mathbf{l}$ ). But, in general, have *mixed* character in 3D.



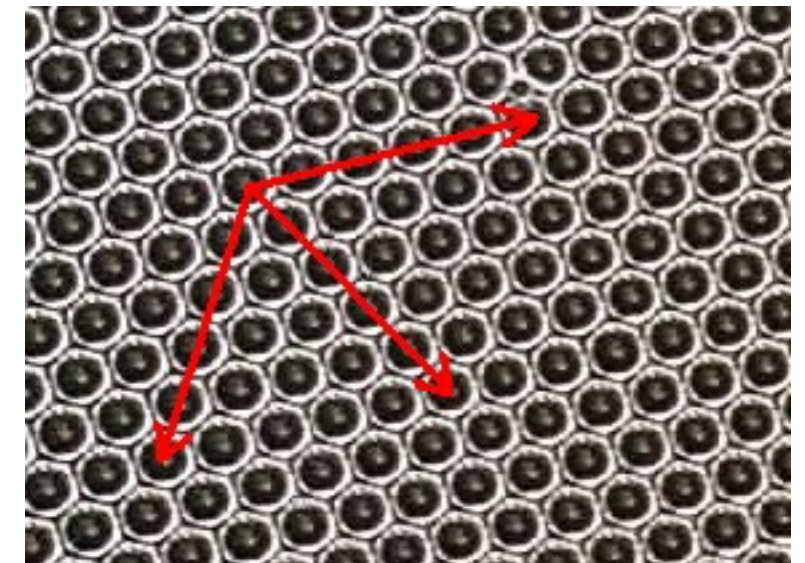
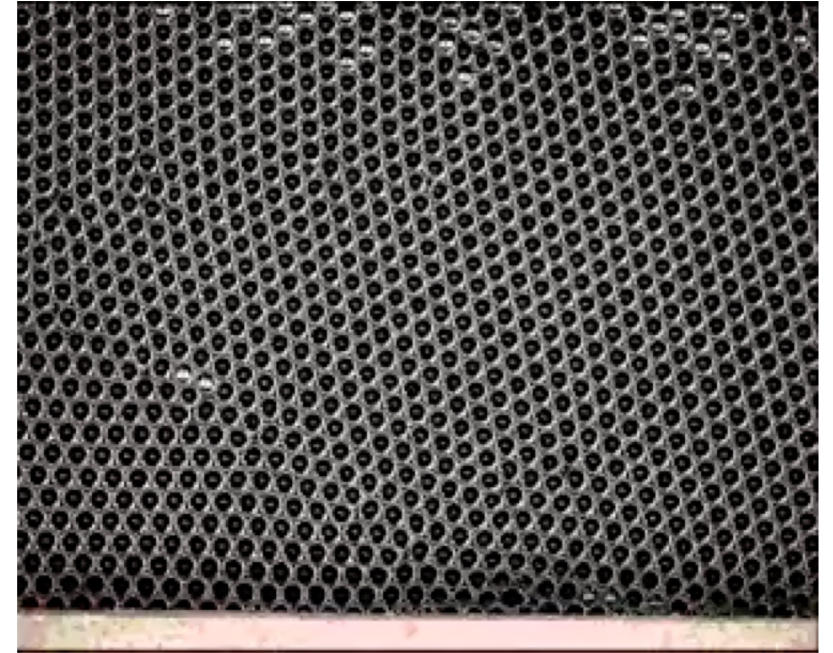


## Slip

- Occurs due to gradual movement of dislocations along specific planes, in specific directions.
- Slip occurs in densely-packed or close-packed planes (lower energy barrier)
- Slip system defined by slip plane and direction.



Movement of edge dislocation under applied shear stress



- Dislocation glide allows plastic deformation at much lower stresses than otherwise required.

## Critically Resolved Shear Stress (CRSS)

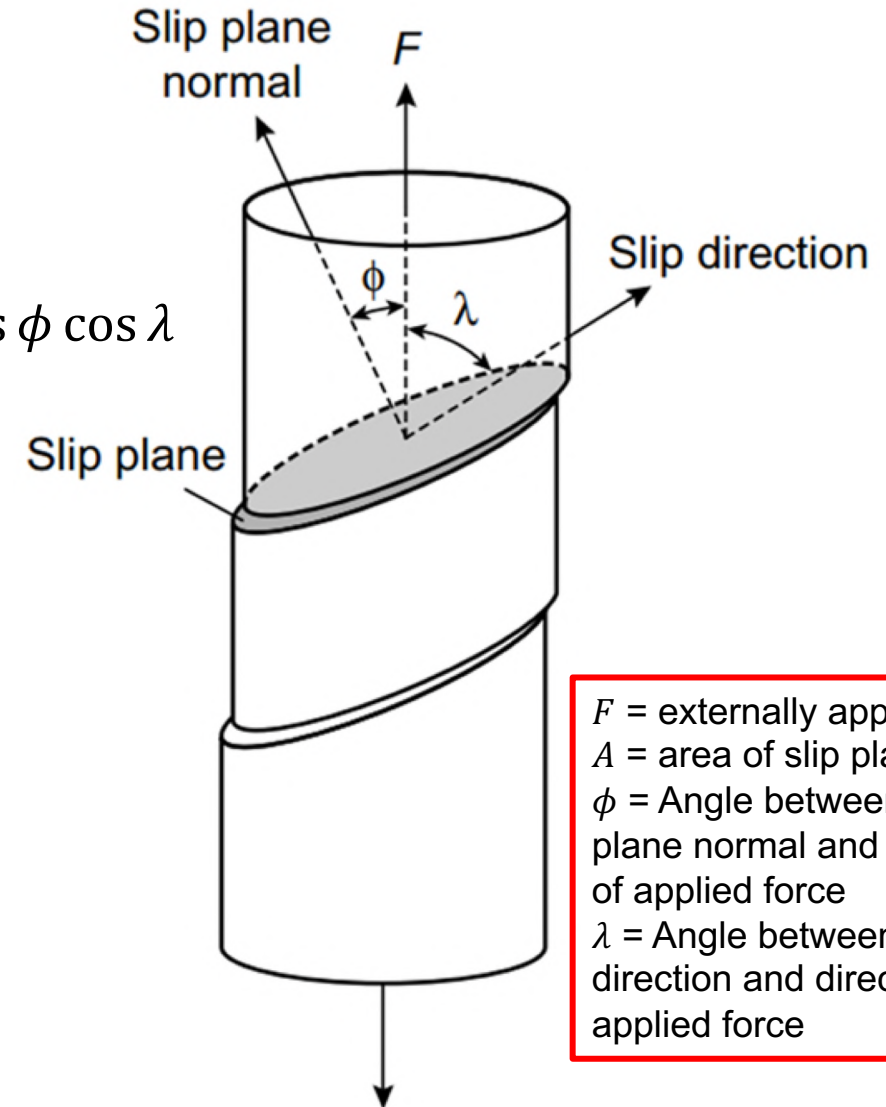
- Resolved shear stress (RSS), acting on slip plane;

$$\tau = \frac{\text{resolved force acting on slip plane}}{\text{area of slip plane}} = \frac{F \cos \lambda}{A / \cos \phi} = \frac{F}{A} \cos \phi \cos \lambda$$

- Critically resolved shear stress (CRSS) of slip plane;

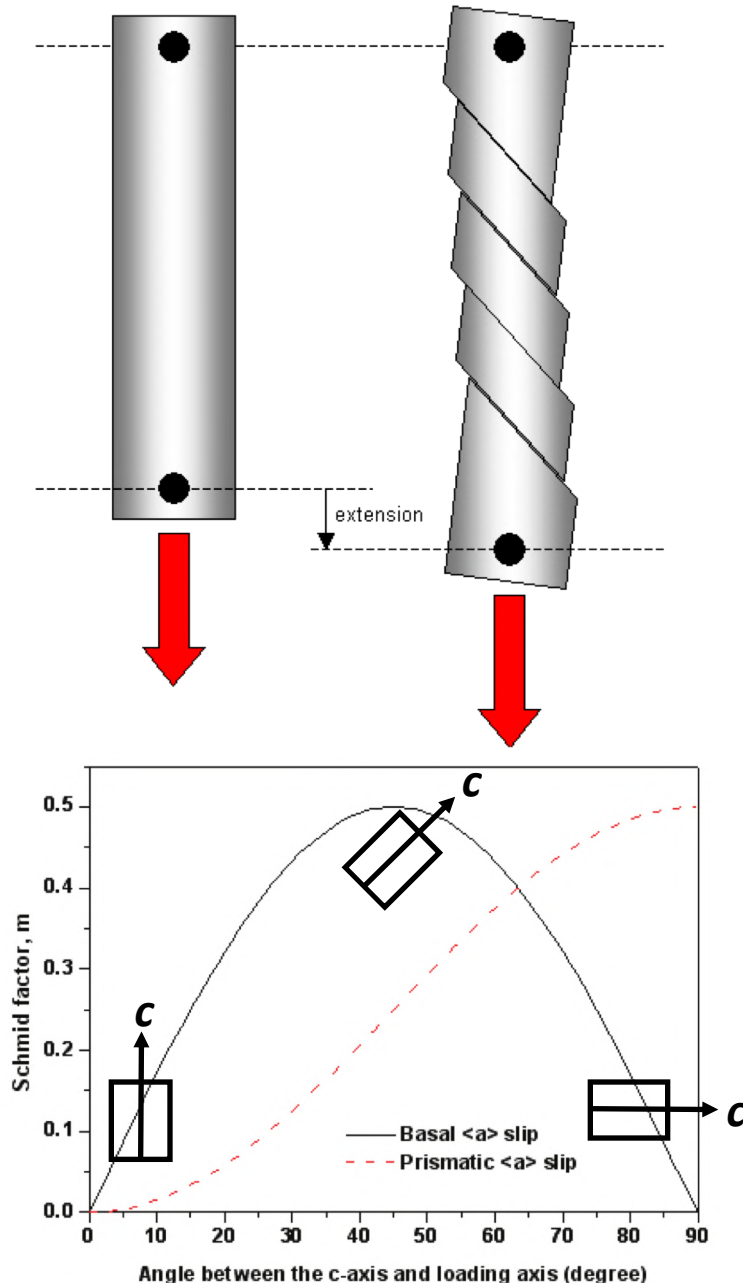
$$\tau_c = \underbrace{\sigma_Y}_{\text{Yield stress}} \underbrace{\cos \phi \cos \lambda}_{\text{Schmid factor}}$$

- If **RSS** > **CRSS**, then slip occurs.



## Grain Rotation

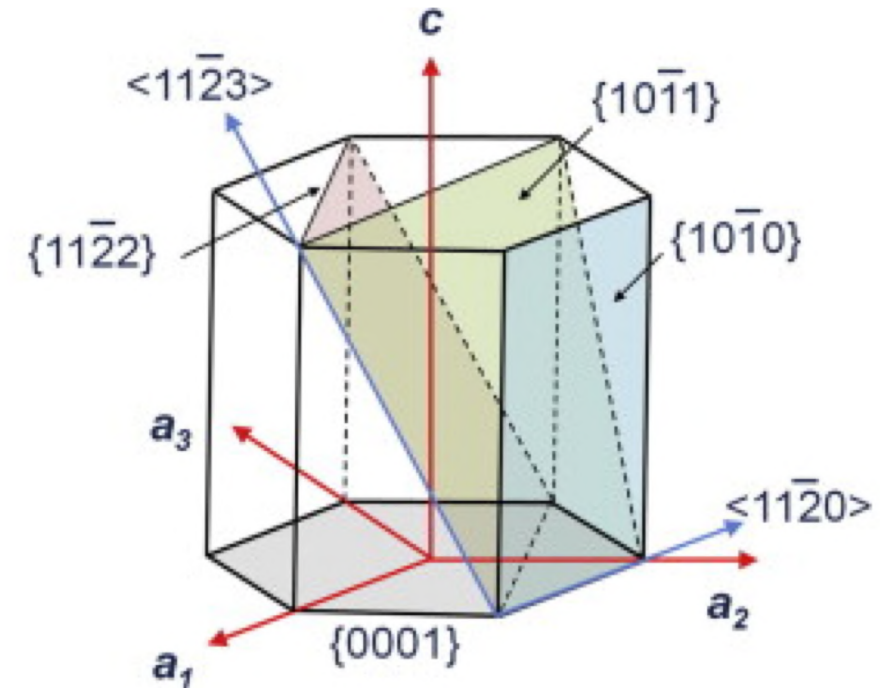
- Slip primarily occurs on grains with highest Schmid factor value.
- In uniaxial tension and compression, slip plane at  $45^\circ$  to loading axis has highest Schmid Factor (soft orientation).
- Edge constraints mean planes cannot glide freely and rotate towards loading axis.
- **Single slip Sachs model** → lattice rotation aligns slip direction with loading axis. *But, this would fracture material.*
- **Multi-slip Taylor model** → number of different slip systems (each with CRSS) accommodate lattice rotation and shape change.



Course goal: Describe deformation and annealing behaviour in terms of slip, twinning and recrystallization mechanisms. And recall the activities of the different slip and twinning systems and how they change with temperature.

## Learning outcomes:

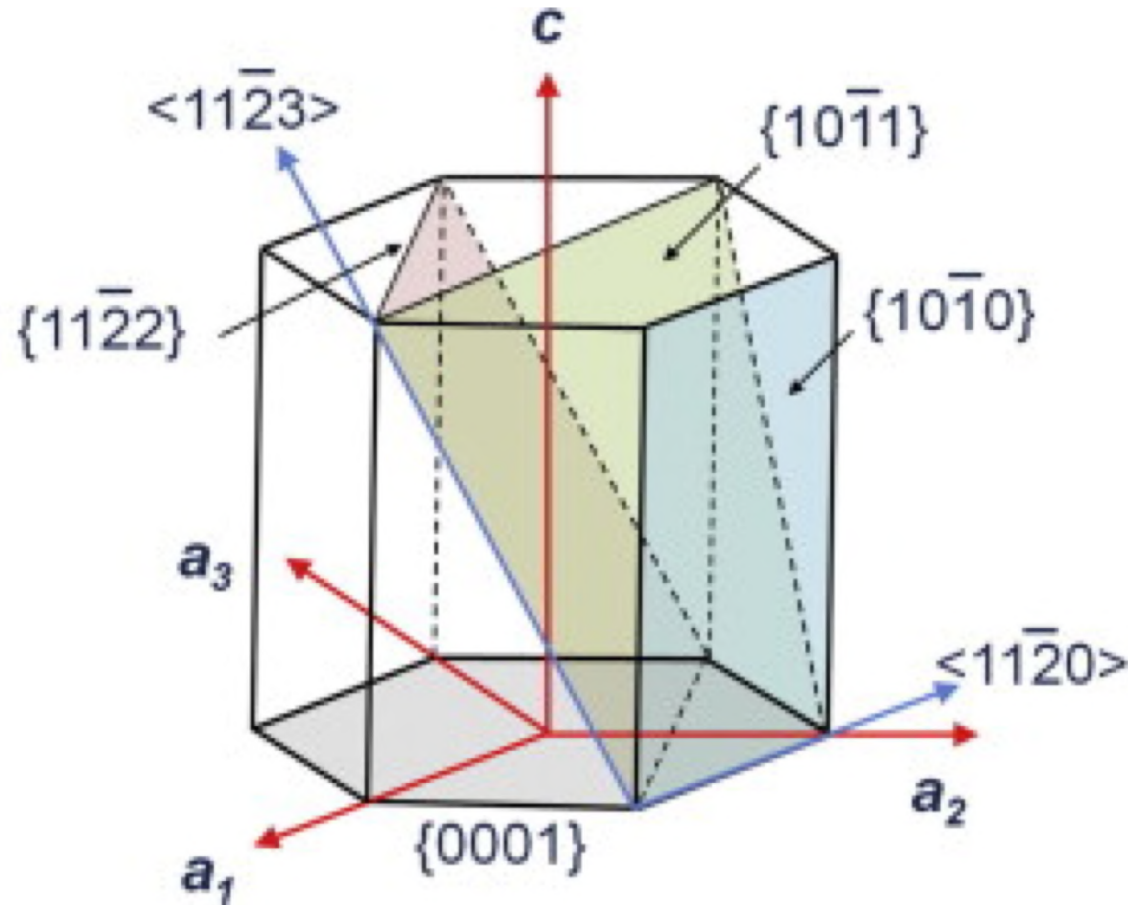
- Explain how slip contributes to grain reorientation and recall equations for RSS, CRSS and Schmid Factor.
- ***Recall the main slip systems in Ti and Zr alloys and how their activities change with temperature.***
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- Describe the driving forces for recrystallization and recovery processes in terms of boundary and stored energy.



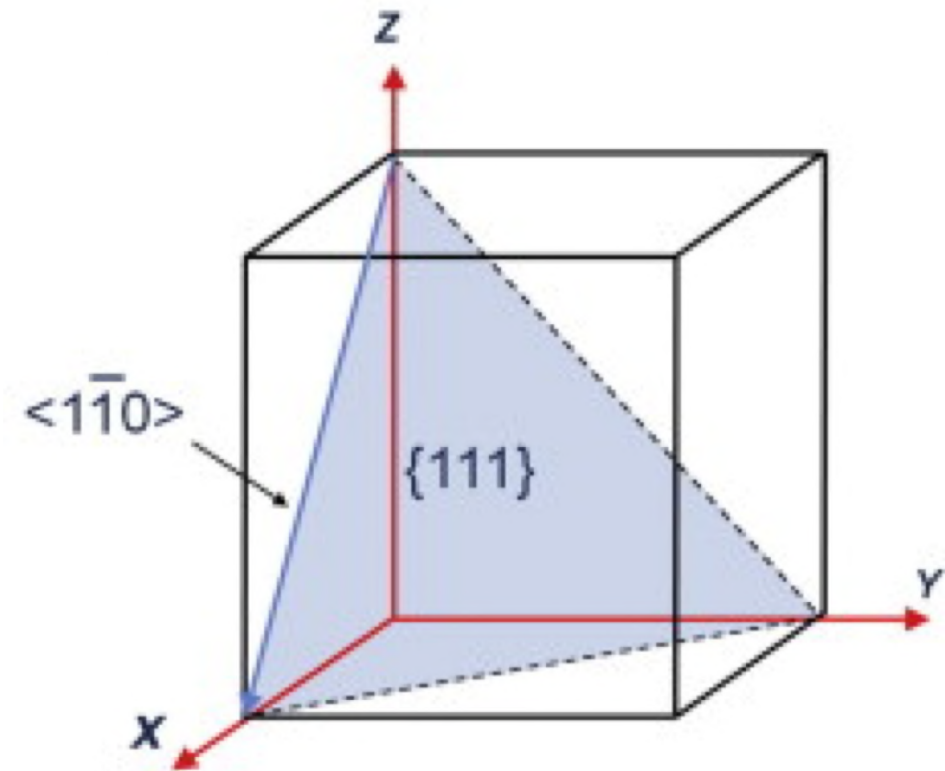
Prismatic, basal and pyramidal slip systems in the HCP phase.



## Deformation in HCP vs FCC Crystal




Fewer slip systems, asymmetrically distributed → **plastic anisotropy**

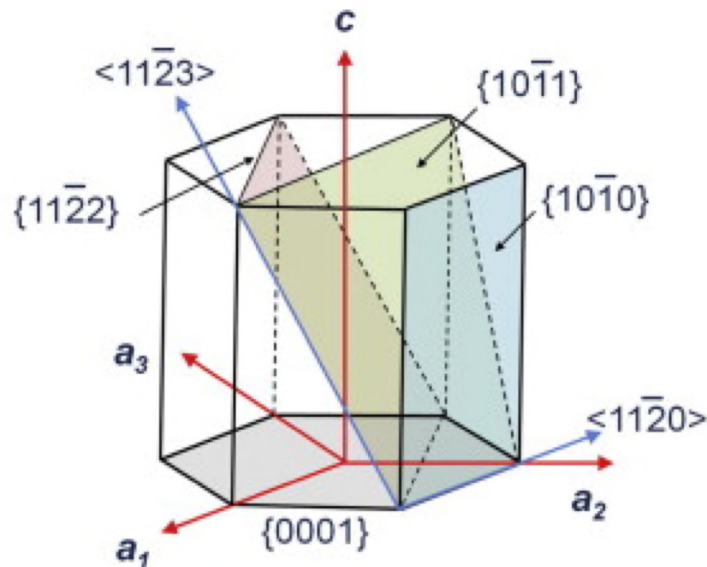


4x  $\{111\}$  planes, each with 3x  $\langle 1\bar{1}0 \rangle$  directions  
= **12 evenly distributed slip systems**

**Both crystal structures close-packed, but HCP deformation is very different.**

## HCP Slip Systems

Slip system type	Slip direction	Slip plane	No. of slip systems		CRSS
			Total	Independent	
Prismatic $\langle a \rangle$	$\langle 11\bar{2}0 \rangle$	$\{10\bar{1}0\}$	3	2	<div>lowest</div> <div style="text-align: center;">  </div> <div>highest</div>
Basal $\langle a \rangle$	$\langle 11\bar{2}0 \rangle$	$\{0002\}$	3	2	
Pyramidal $\langle a \rangle$	$\langle 11\bar{2}0 \rangle$	$\{10\bar{1}1\}$	6	4	
Pyramidal $\langle c + a \rangle$	$\langle 11\bar{2}3 \rangle$	$\{11\bar{2}2\}$	6	5	

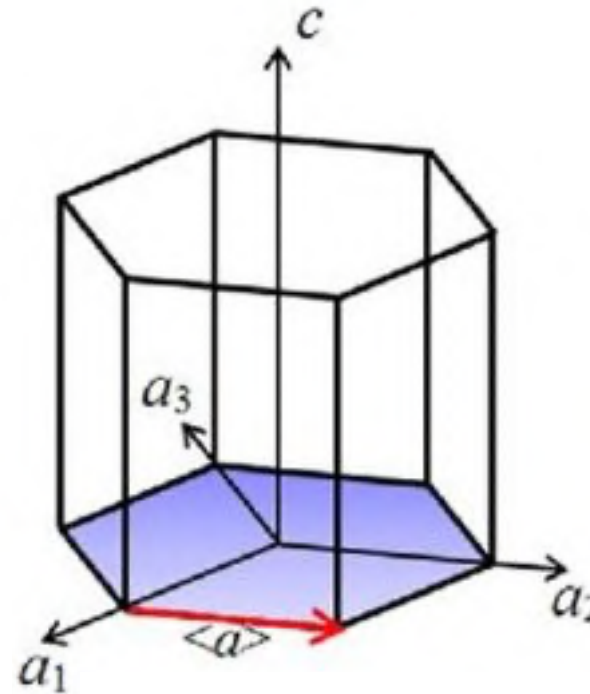


*According to the Von-Mises criterion, homogeneous deformation of a polycrystalline material requires 5 independent slip systems.*

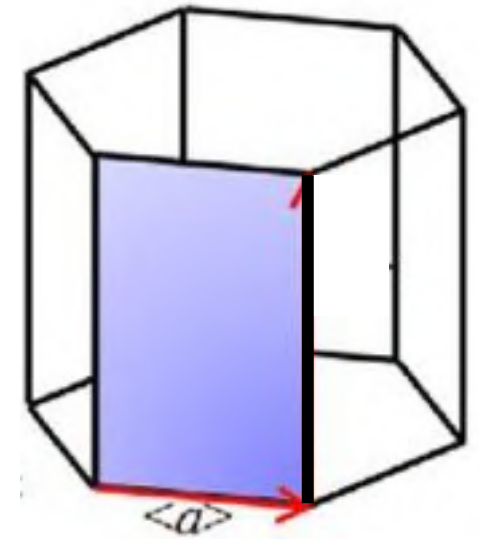


## Prismatic vs Basal $\langle a \rangle$ Slip

- *Live lecture – Why is prismatic  $\langle a \rangle$  slip easier than basal  $\langle a \rangle$  slip?*
- Ideal  $c/a$  ratio: 1.633
- Zr  $c/a$  ratio: 1.593
- Ti  $c/a$  ratio: 1.587



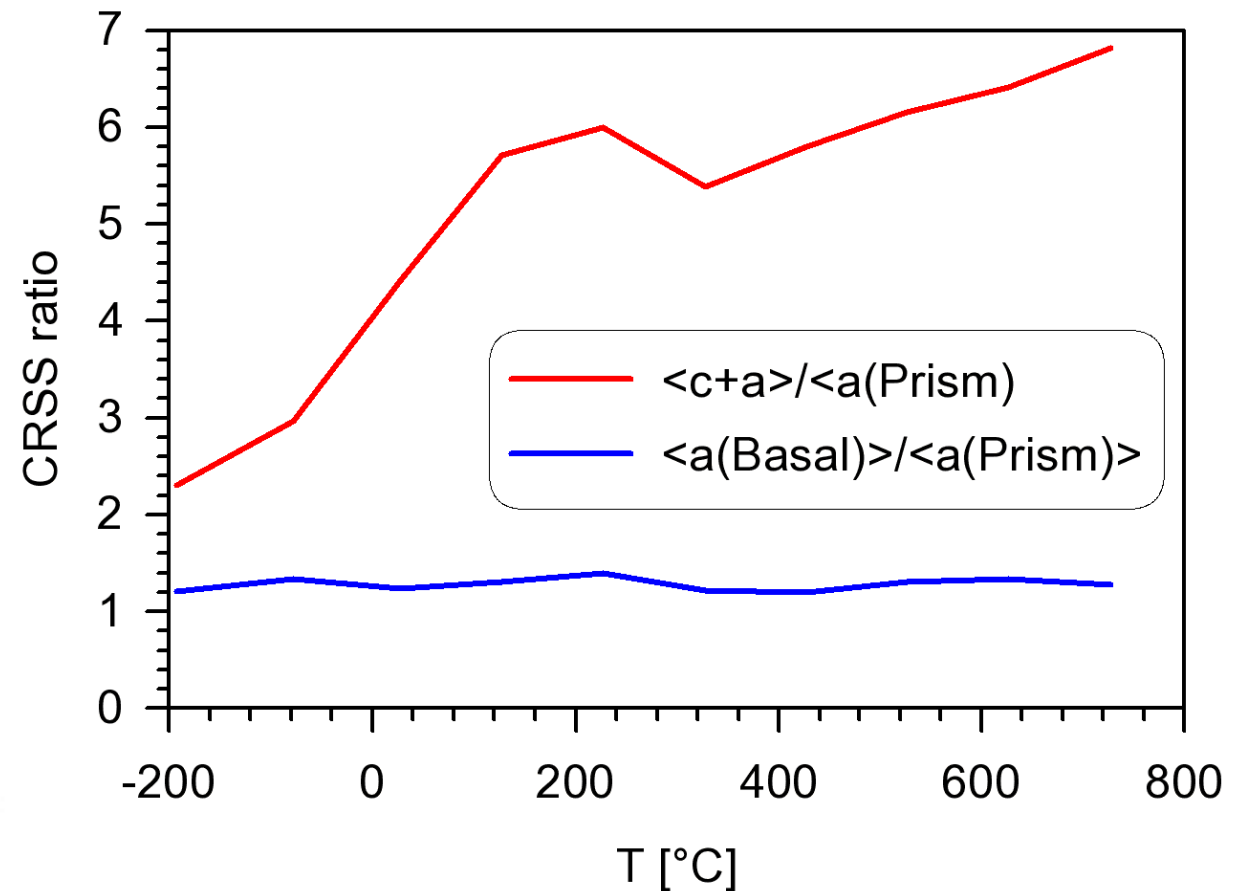
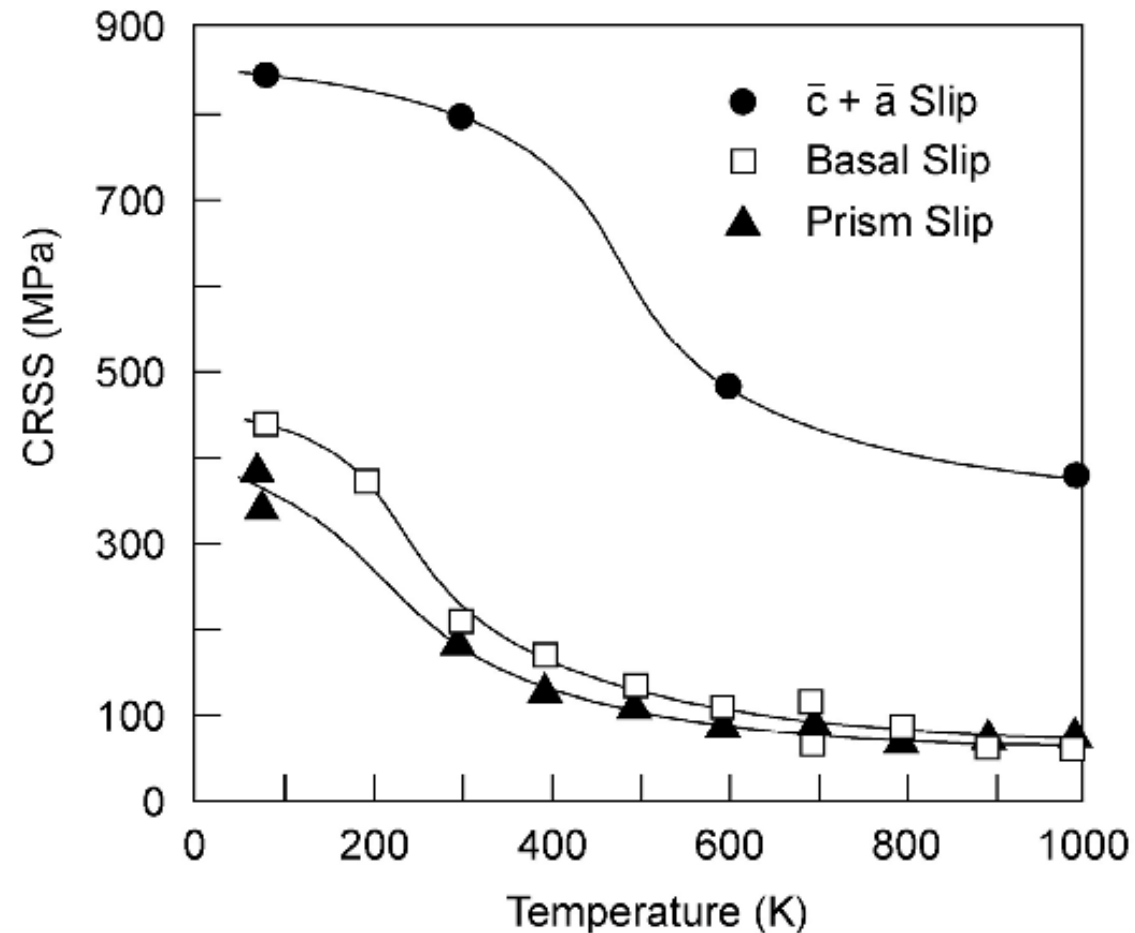
Basal Slip  
 $\frac{1}{3} \langle 11\bar{2}0 \rangle (0002)$



Prismatic Slip  
 $\frac{1}{3} \langle 11\bar{2}0 \rangle \{10\bar{1}0\}$

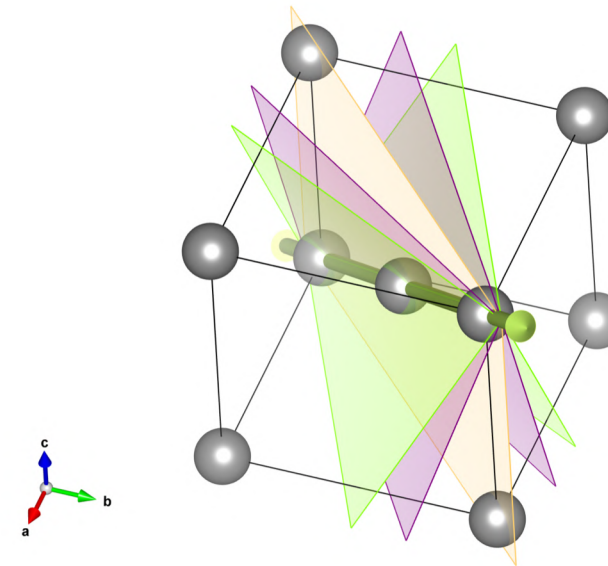
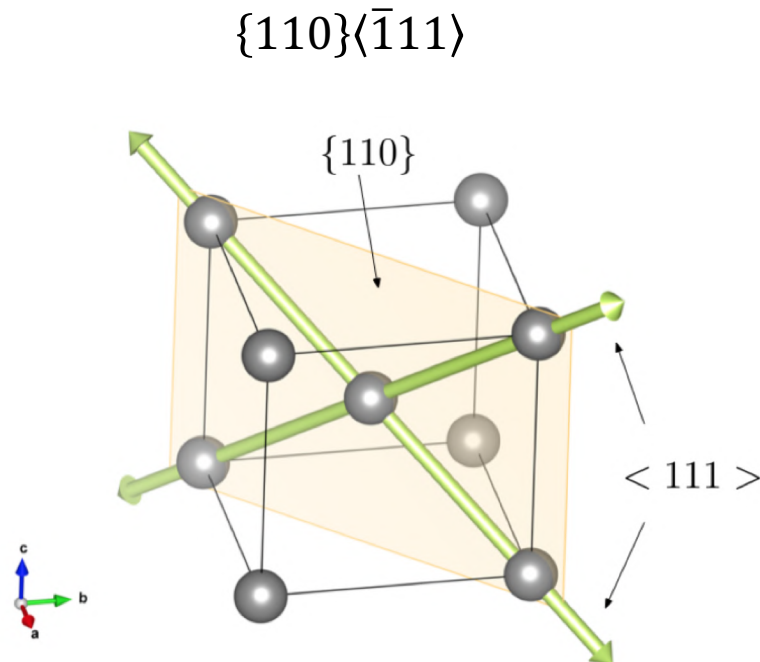
## Slip Activity with Temperature

- CRSS values for Ti-6Al...



## Slip in $\beta$ -phase

- Slip along close-packed  $\langle 111 \rangle$  direction.
- Different planes can accommodate slip  $\rightarrow$  pencil glide.

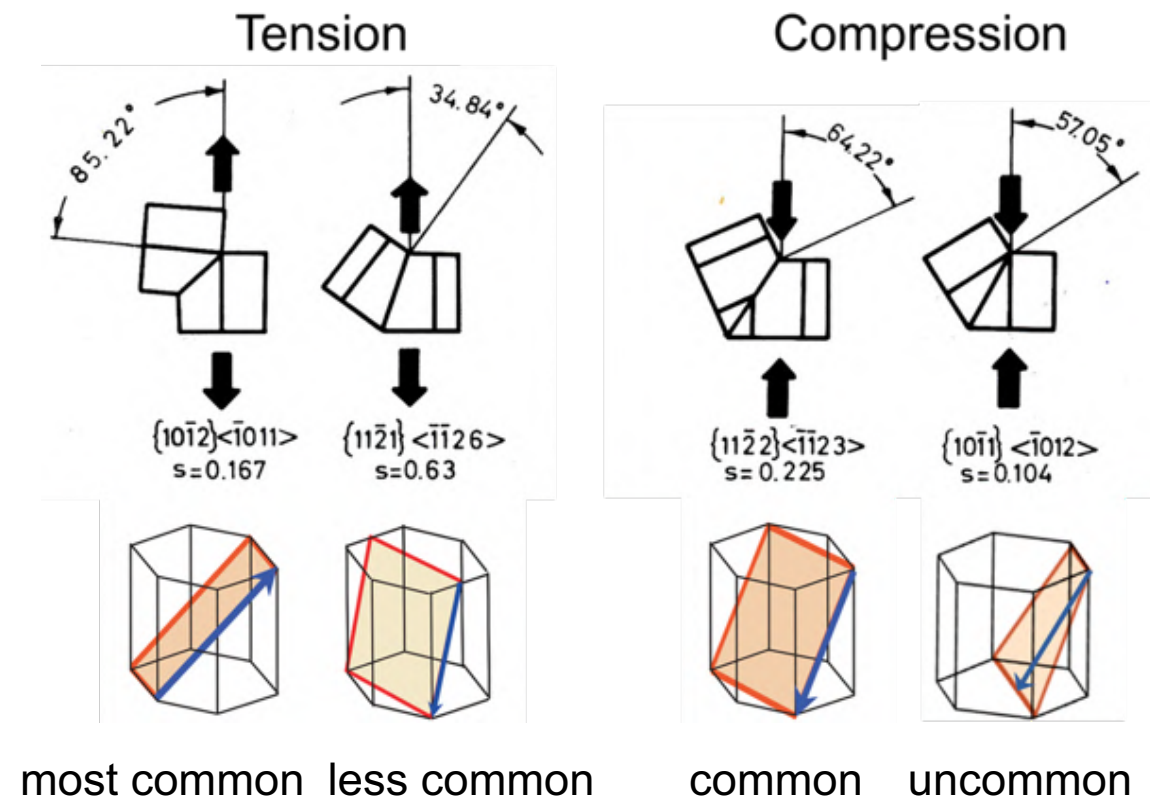




Course goal: Describe deformation and annealing behaviour in terms of slip, twinning and recrystallization mechanisms. And recall the activities of the different slip and twinning systems and how they change with temperature.

## Learning outcomes:

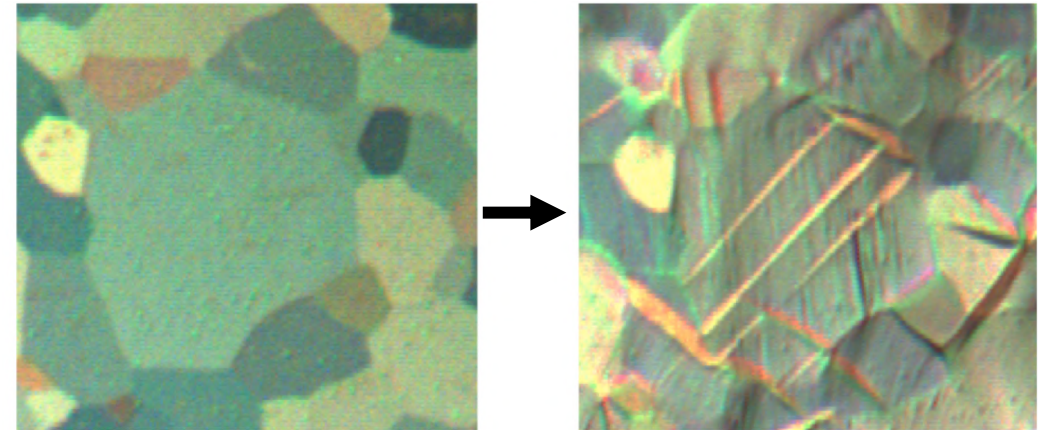
- Explain how slip contributes to grain reorientation and recall equations for RSS, CRSS and Schmid Factor.
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- **Explain how twinning contributes to grain reorientation and recall the main twinning types in Ti and Zr alloys.**
- Describe the driving forces for recrystallization and recovery processes in terms of boundary and stored energy.



The main twinning types in Ti and Zr alloys.

## Twinning Appearance

- Twins appear as thin lens-shaped structures.
- Characterised by specific misorientation with parent crystal.



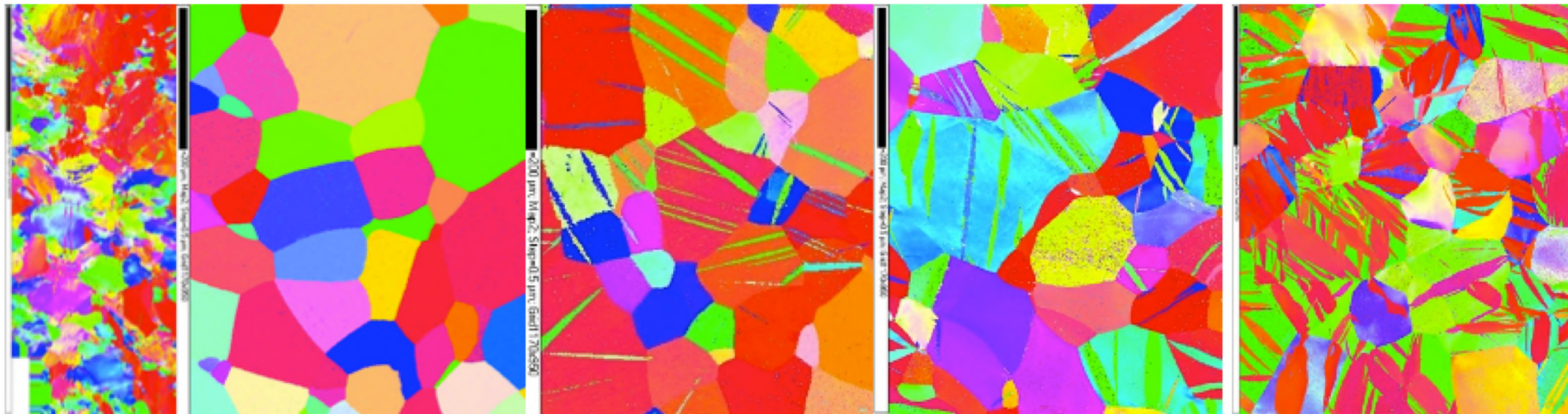
As rolled

Initial state

1.7%

3.7%

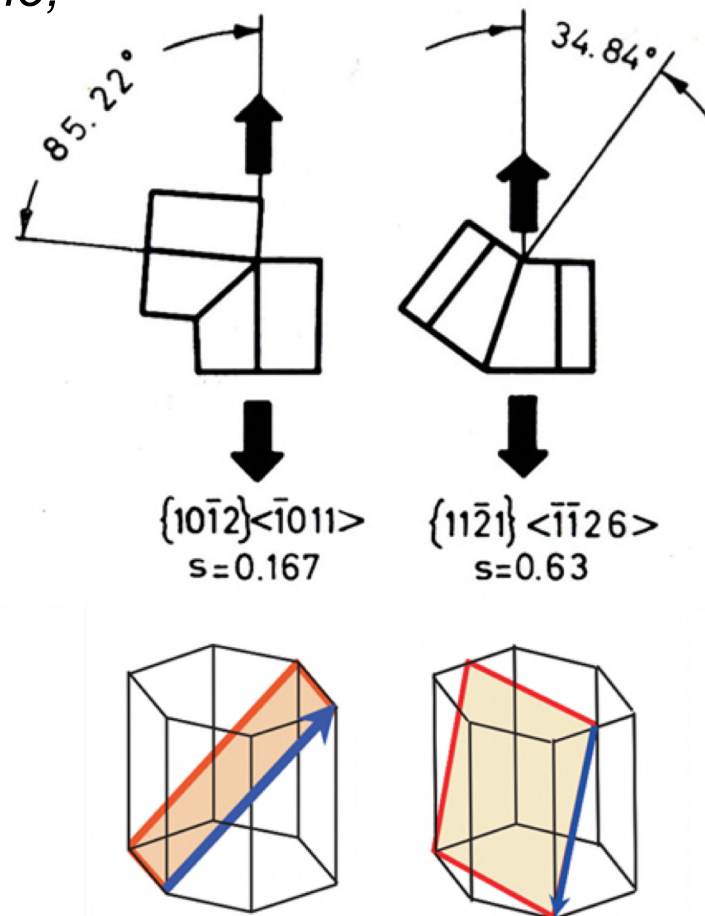
8.7%



## Twinning Types

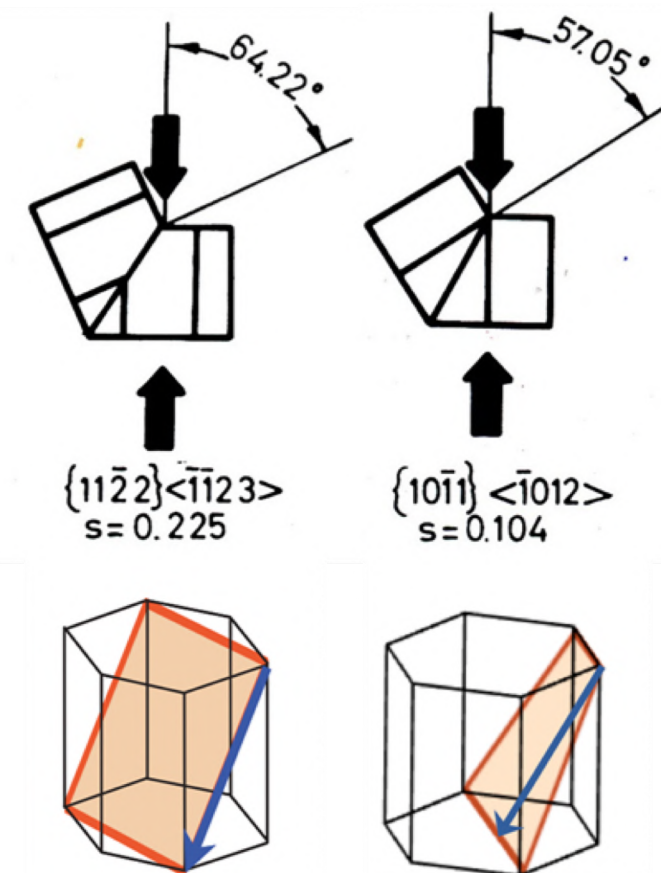
- When insufficient slip systems available, deformation can occur via twinning.
- Atoms reshuffling (small distances) results in grain rotation, with significant shear strain.
- Provides shear with  $\langle c \rangle$  component.
- **Tension twin:**  $\langle c \rangle$  axis in tension, rotates towards compression
- **Compression twin:**  $\langle c \rangle$  axis in compression, rotates toward tension

Tension



most common    less common

Compression

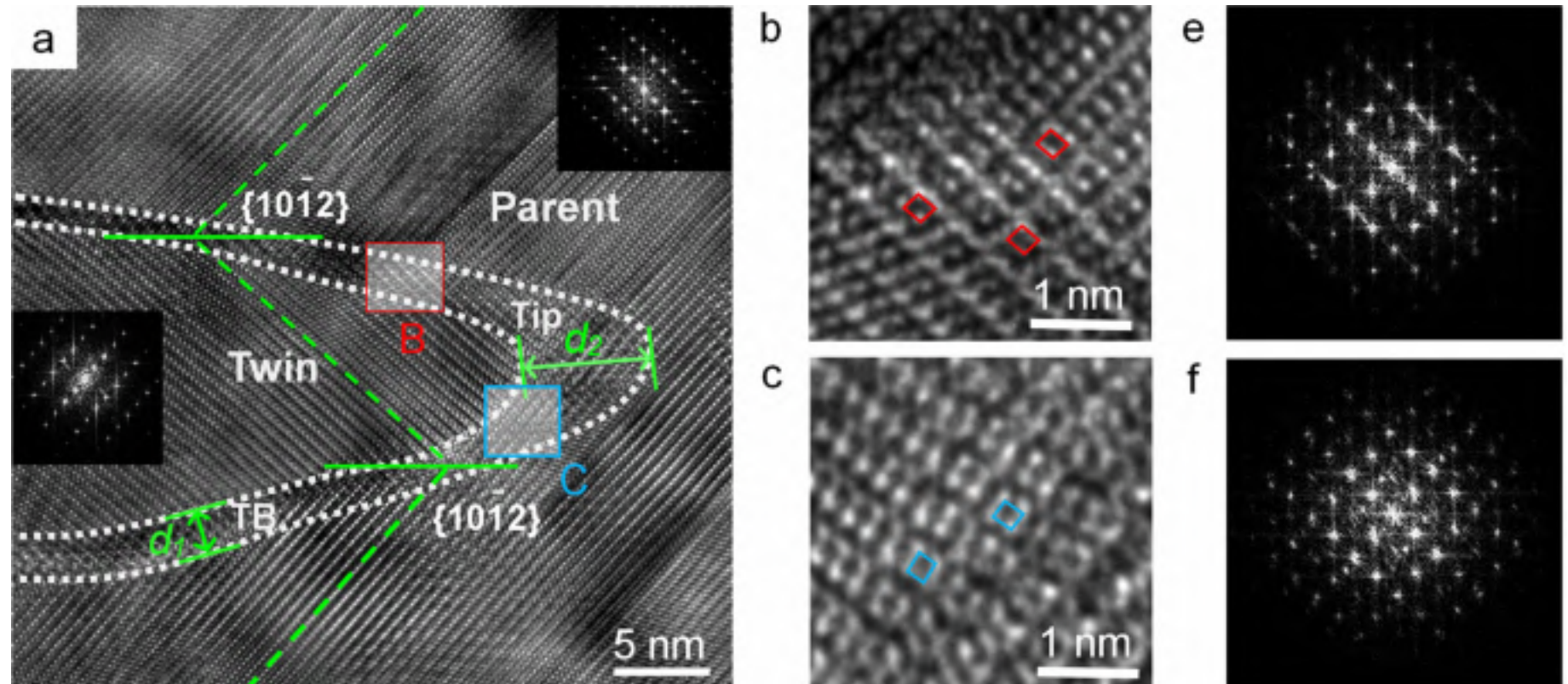


common    uncommon



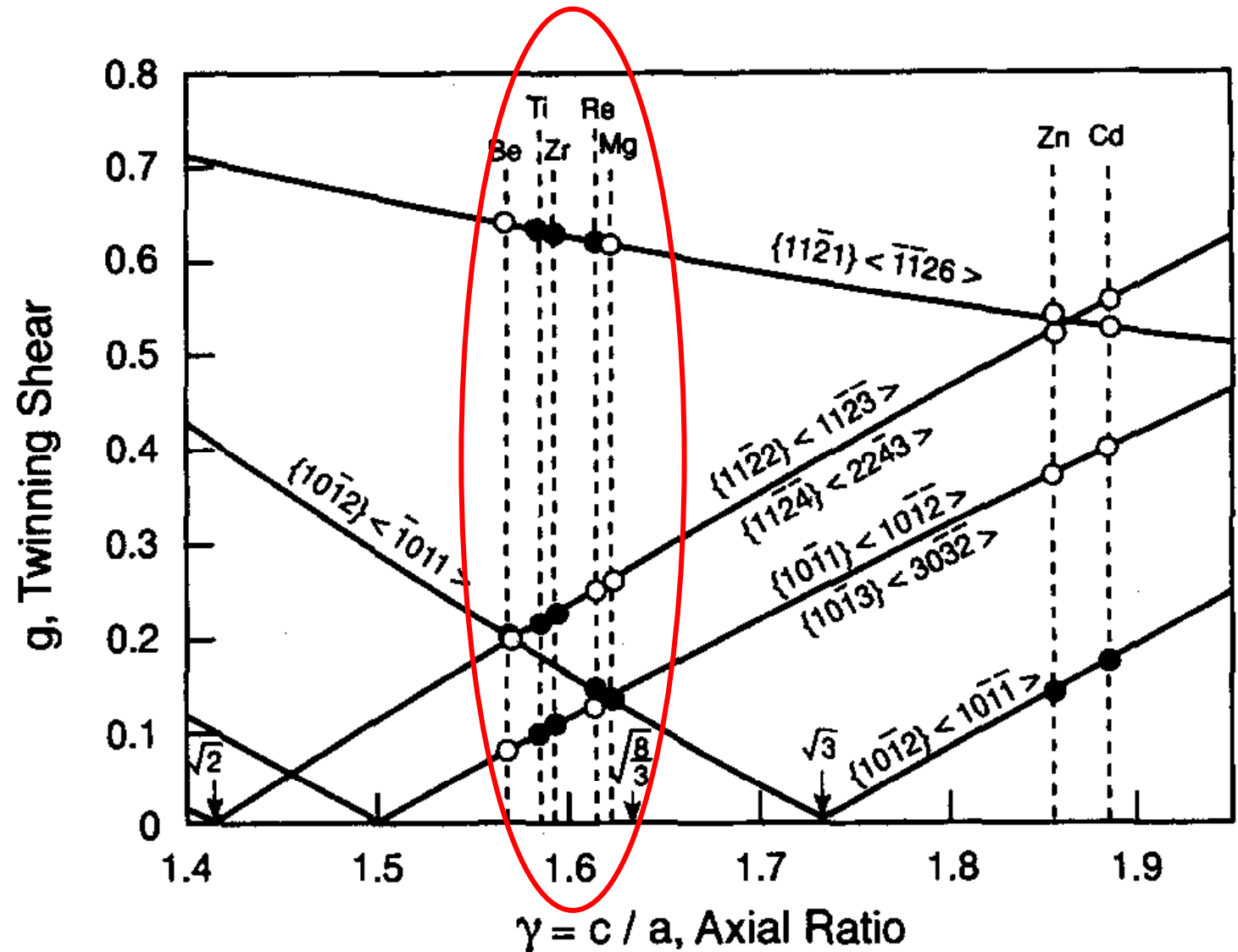
## Twinning Image

- Using TEM, we can see the new crystallographic alignment of atoms within the twin.



## Twinning Shear

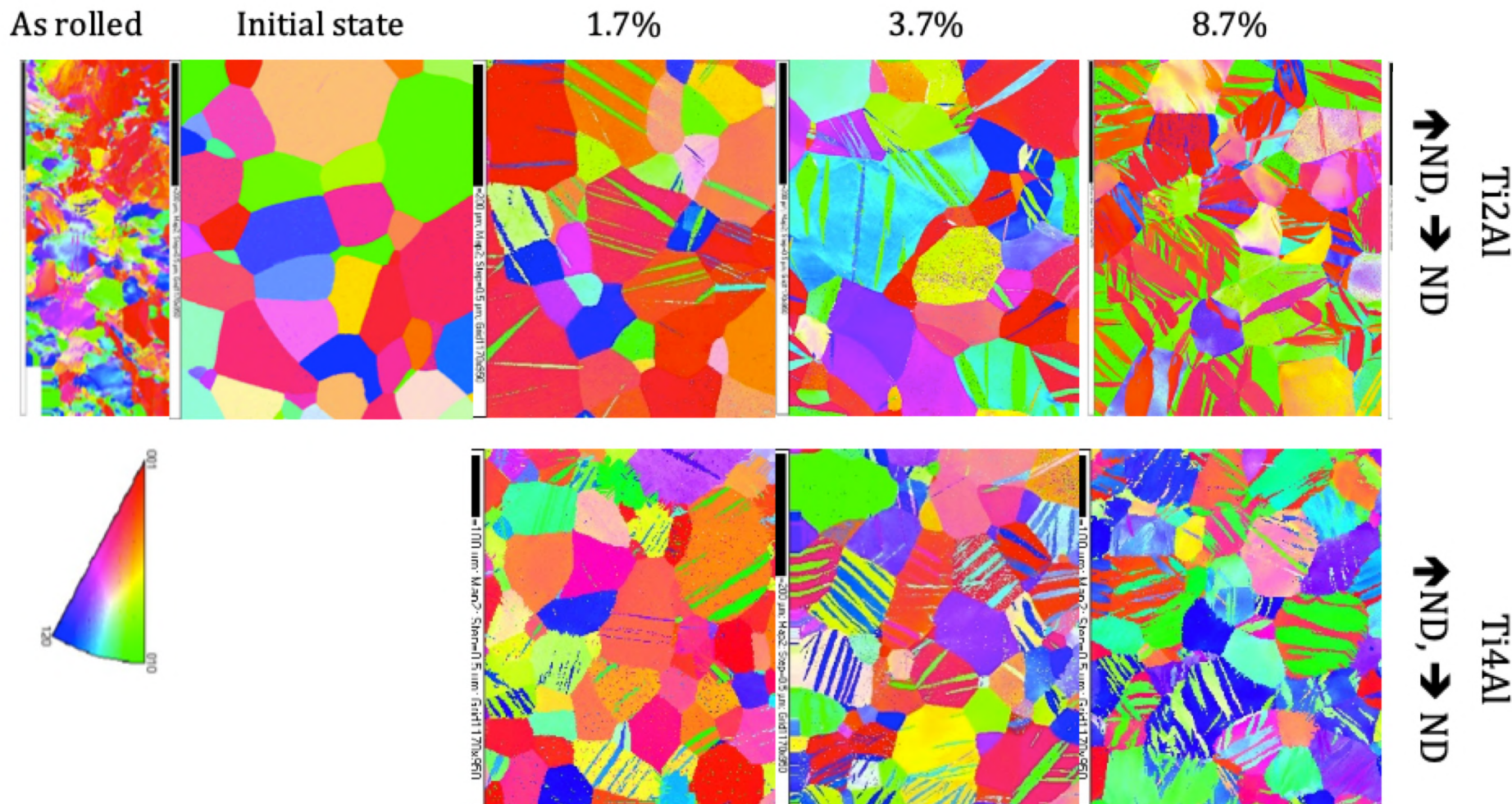
- Crystallography determines the twinning shear.
- ↓
- $c/a$  ratio characterises the twinning shear of the crystal.





# Twinning with Strain and Temperature

- **Strain:** Twinning tends to only occur at low strains, which align grains for further slip.
- **Temperature:** Twinning reduces at higher deformation temperatures.
- *But, tensile and compression twinning has been reported at  $>550^{\circ}\text{C}$  in Zr alloys.*



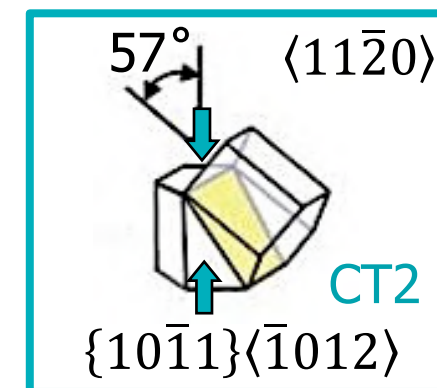
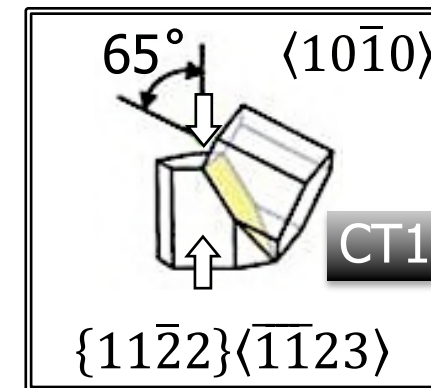
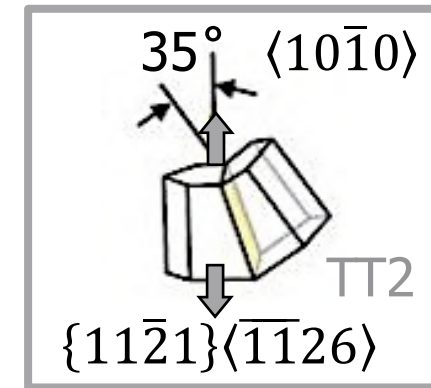
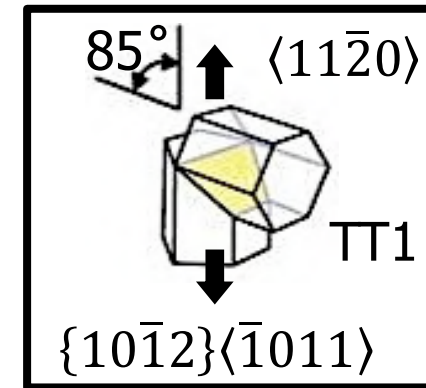
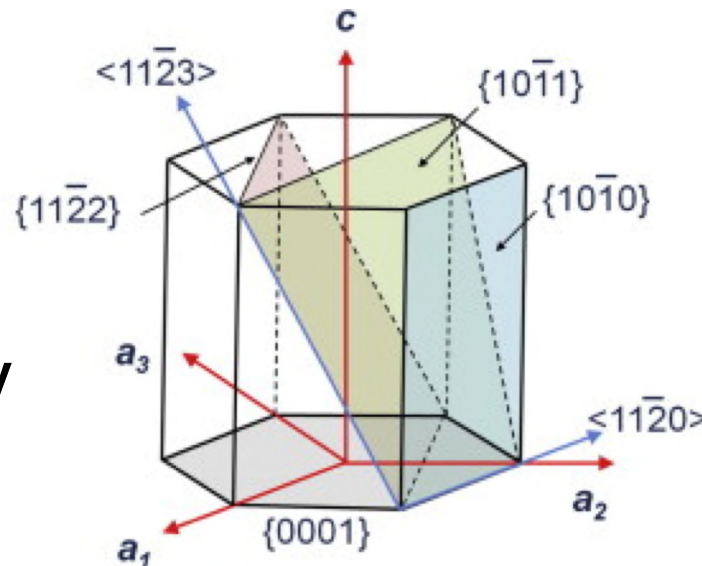


## Why is Slip and Twinning Important?

- HCP lattice in Ti and Zr alloys;
- *Elastically and plastically anisotropic.*
- *Low offer of slip systems.*
- *Asymmetrical distribution of slip systems.*
- *Strict crystallographic orientation relationships for twinning.*

• Therefore...

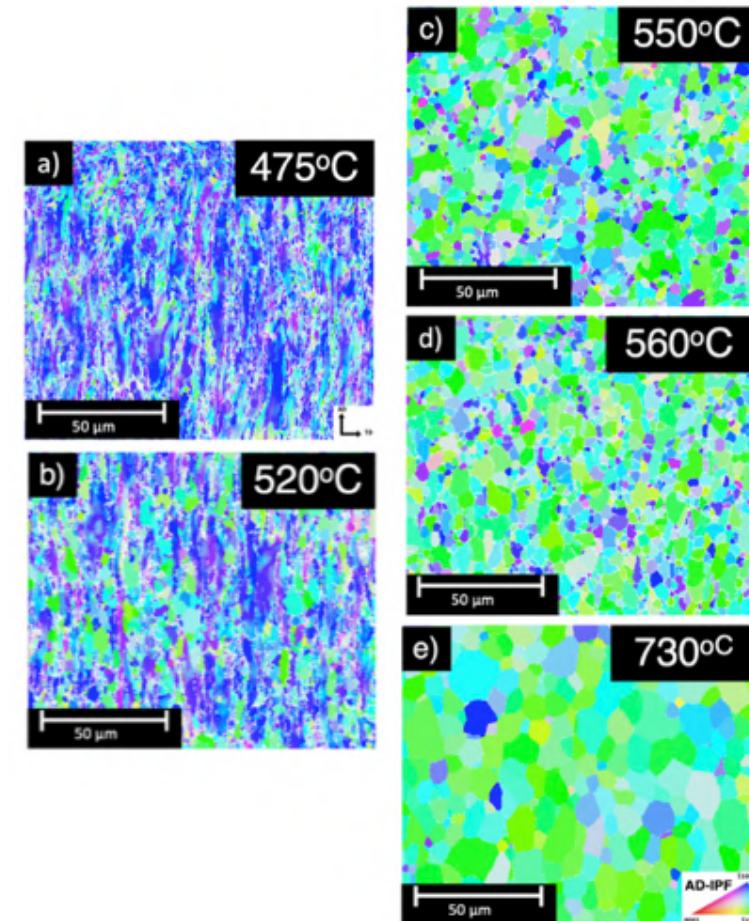
- **Strong deformation texture (crystallographic orientation).**
- **Strong mechanical anisotropy in-service.**



Course goal: Describe deformation and annealing behaviour in terms of slip, twinning and recrystallization mechanisms. And recall the activities of the different slip and twinning systems and how they change with temperature.

## Learning outcomes:

- Explain how slip contributes to grain reorientation and recall equations for RSS, CRSS and Schmid Factor.
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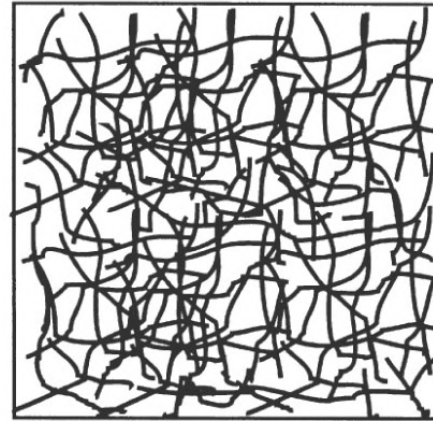
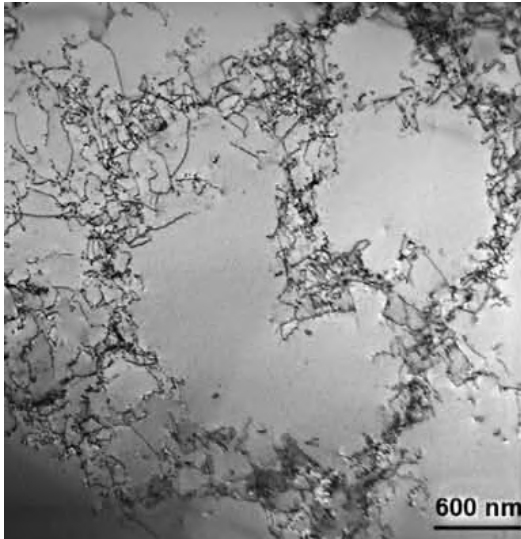


EBSD images showing the effect of annealing at different temperatures, forming fully recrystallized grains at higher temperatures.

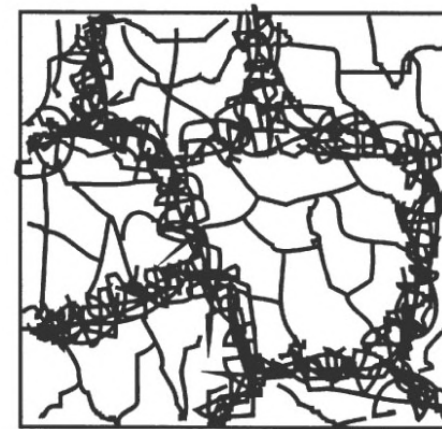
## Recovery

*Ti and Zr materials undergo changes during annealing;*

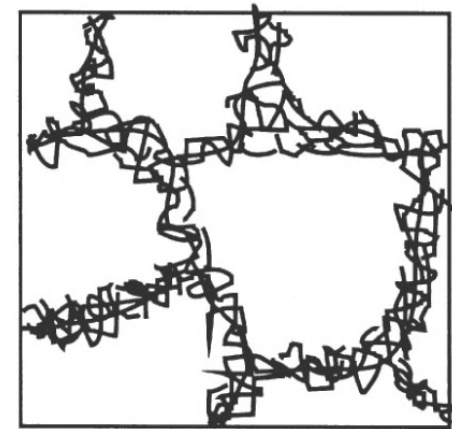
- **Recovery:** dislocations annihilate and rearrange, forming new substructures.
- Driven by reduction in boundary area.



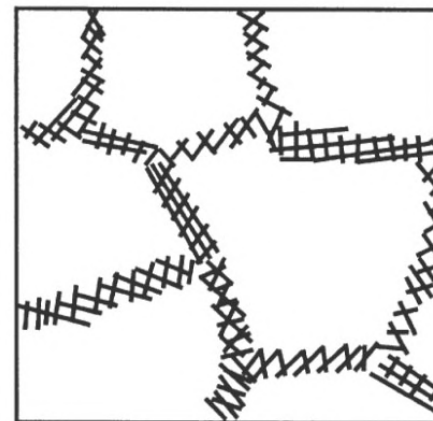
(a) Dislocation tangles



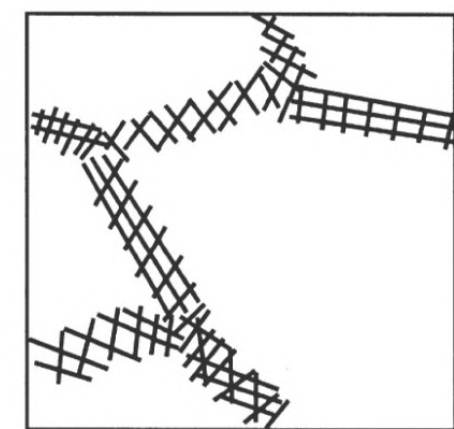
(b) Cell formation



(c) Annihilation of dislocations within cells



(d) Subgrain formation



(e) Subgrain growth



# Recrystallization and Grain Growth

*Ti and Zr materials undergo changes during annealing;*

- **Recrystallization:** new dislocation-free grains within deformed structure.
- New grains have **stored energy** advantage to consume old grains;

$$E_D = c\rho Gb^2 \text{ and } E_D \approx \frac{3\gamma_s}{D} \approx \frac{K\theta}{D}$$

$E_D$  = Stored energy per volume

$c$  = constant,  $\sim 0.5$

$\rho$  = dislocation density

$G$  = shear modulus

$b$  = Burgers vector

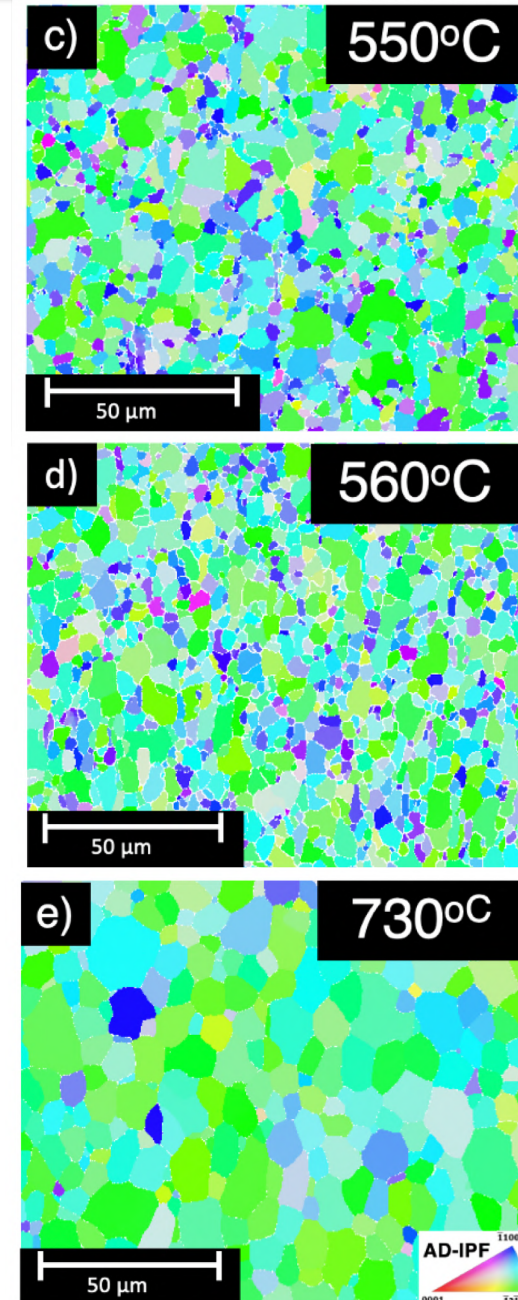
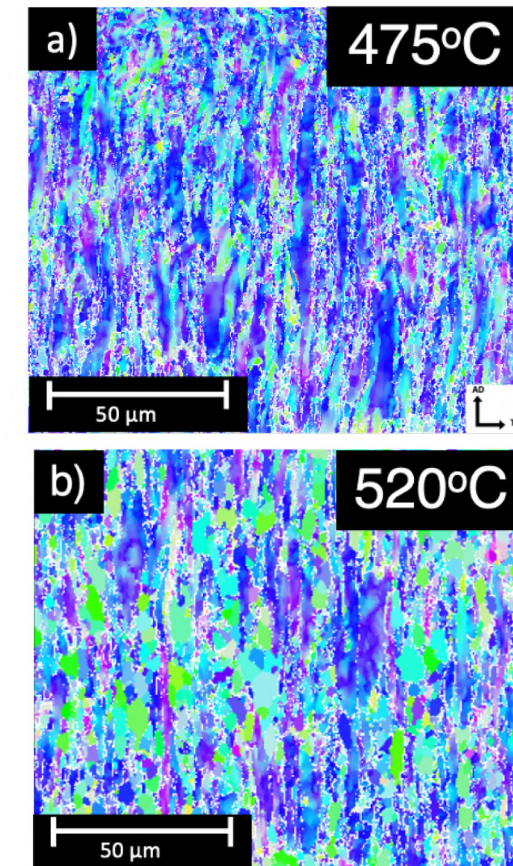
$\gamma_s$  = boundary energy

$D$  = subgrain diameter

$K$  = constant

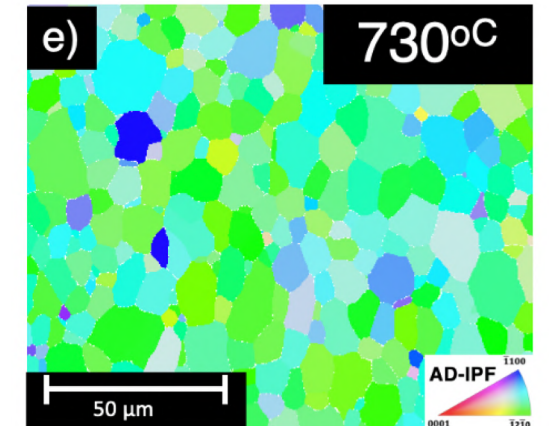
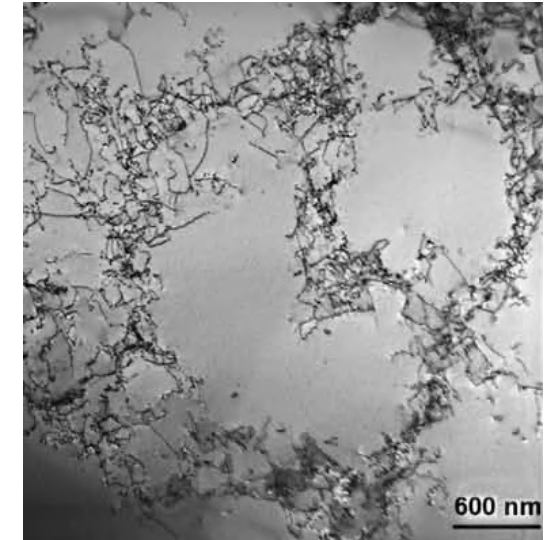
$\theta$  = boundary misorientation

- **Grain Growth:** Growth of larger grains, driven by lowering boundary area.



## Stacking Fault Energy (SFE)

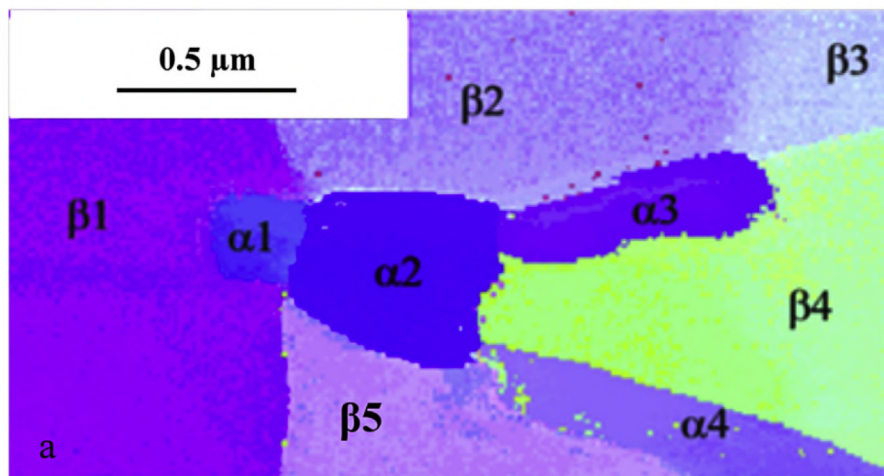
- Stacking Fault Energy (SFE) – Related to atomic bonding in material.  
Determines dissociation of dislocations.
- High SFE** → Full dislocations.  
Promotes climb, cross-slip and annihilation.  
(*Recovery*)
- Low SFE** → Dissociation into partial dislocations.  
Hinders recovery and promotes new grains forming.  
(*Recrystallization*)
- In Zr and Ti alloys,
  - some dislocation types have high SFE and some have low SFE.
  - recrystallization favoured at grain boundaries and twinned sites.



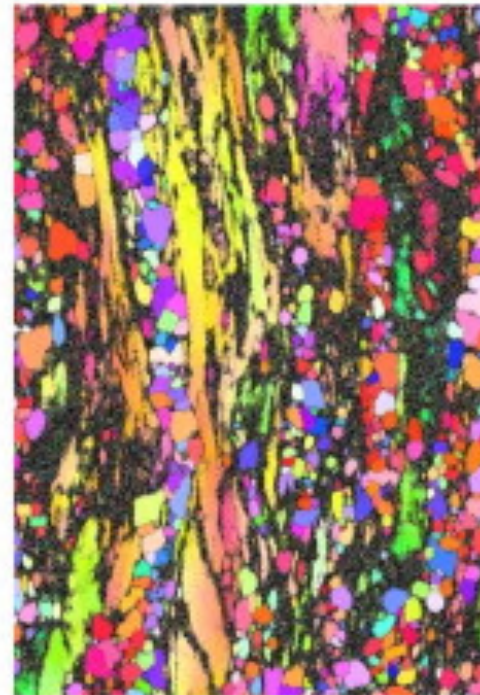


# Dynamic Recovery and Dynamic Recrystallization

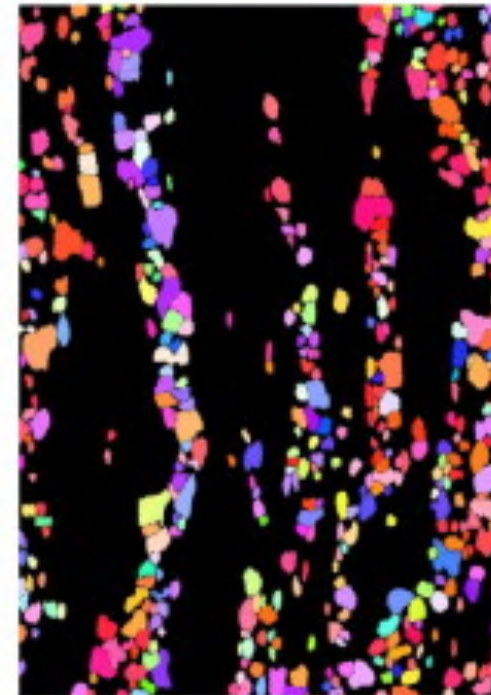
- In Zr and Ti alloys which are processed at higher temperatures...
- Processes of Recovery and Recrystallization can occur during high temp. deformation (dynamically).



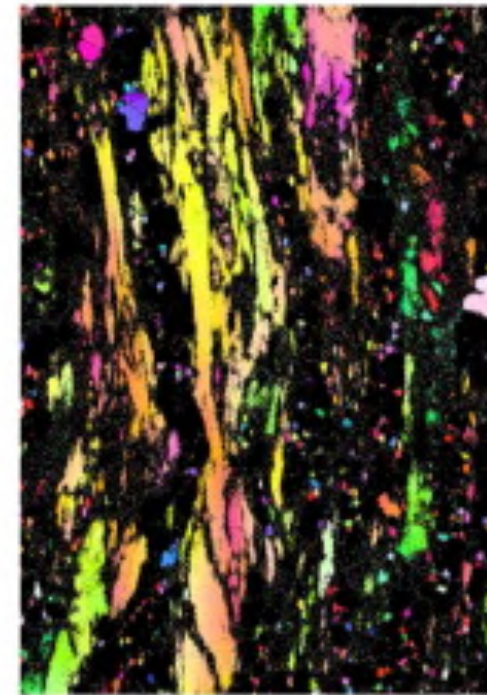
Pilgered/part-annealed



Recrystallized grains



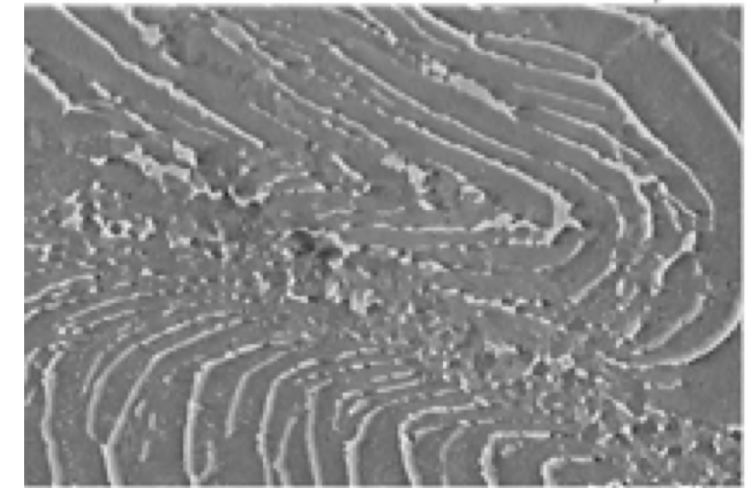
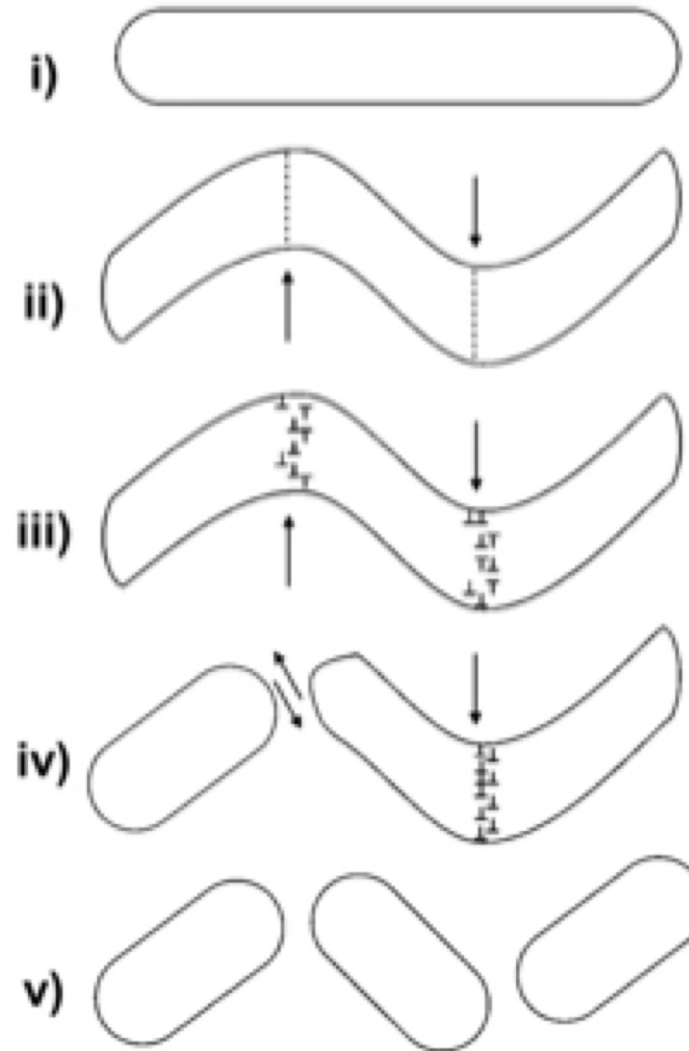
Deformed grains



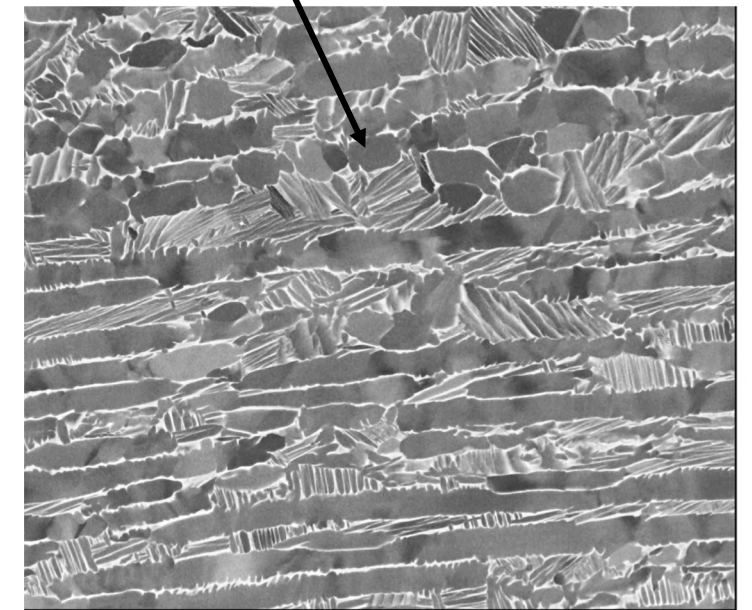
→ Resulting in new spheroidised grains / orientations forming during deformation.

## Globularisation

- i) Starting  $\alpha$ -lath
- ii) Deformation band formation
- iii) Dislocation formation and rearrangement (via recovery)
- iv)  $\beta$ -phase ingress at points of high dislocation density
- v) Spheroidised  $\alpha$ -grains



Spheroidised grains after cooling.





## Dynamic Transformation

- On top of this, new observations also show phase transformation during processing (dynamic transformation).
- All of these processes make analysing and modelling microstructure and texture evolution in Zr and Ti alloys a very interesting job!

